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Karmarkar

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[54] METHODS AND APPARATUS FOR
EFFICIENT RESOURCE ALLOCATION

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[57] ABSTRACT

A method and apparatus for optimizing resource alloca-
tions is disclosed which proceeds in the interior of the
solution space polytope instead of on the surface (as
does the simplex method), and instead of exterior to the
polytope (as does the ellipsoid method). Each suc-
cessive approximation of the solution point, and the poly-
tope, are normalized such that the solution point is at
the center of the normalized polytope. The objective
function is then projected into the normalized space and
the next step is taken in the interior of the polytope, in
the direction of steepest-descent of the objective func-
tion gradient and of such a magnitude as to remain
within the interior of the polytope. The process is re-
peated until the optimum solution is closely approxi-
mated. The optimization method is sufficiently fast to be
useful in real time control systems requiring more or
less continual allocation optimization in a changing
environment, and in allocation systems heretofore too
large for practical implementation by linear program-
ming methods.

36 Claims, 5 Drawing Sheets

